Study Programme: Applied Mathematics - Data Science

Course Unit Title: Statistics theory for learning and signal processing

Course Unit Code: MДC17

Name of Lecturer(s): Danijela Rajter-Ćirić

Type and Level of Studies: Master Academic Degree

Course Status (compulsory/elective): Elective

Semester (winter/summer): Summer

Language of instruction: English

Mode of course unit delivery (face-to-face/distance learning): Face-to-face

Number of ECTS Allocated: 6

## **Prerequisites:**

Basics of linear algebra and probability

## **Course Aims:**

- Understanding of a wide range of statistical metrics, methods, and analytical techniques for machine learning and signal processing

# **Learning Outcomes:**

- Ability to select a suitable statistical method for a given research problem

- Ability to apply the taught statistical methods on a given research problem
- Ability to validate/assess, and give guarantees, for various machine learning/signal processing

approaches based on the taught statistical metrics

# Syllabus:

Theory

Estimation: Minimum variance unbiased estimation, Cramer-Rao lower bound, Maximum likelihood estimation, Bayesian estimation, Unbiasedness, Asymptotic efficiency, Asymptotic normality; Detection: Binary hypothesis testing, M-ary hypothesis testing, Neyman-Pearson optimal detection, Average error probability-optimal detection; Concentration inequalities: Markov, Chebyshev, Chernoff, Hoeffding, Efron-Stein; Large deviations: Cramer theorem, Gartner-Ellis theorem, Stein's lemma, Chernoff's lemma; Minimax theory: Le Cam's method, Fano's method; Risk minimization: Tsybakov's noise conditions, Surogate loss functions.

Practice

Application examples in telecom, electric grid (smart grid), machine learning, sensor networks, etc.

# **Required Reading:**

Selected parts of the following books:

14. Larry Wasserman: All of Statistics: A Concise Course in Statistical Inference, Springer, 2014

15. Harry L. Van Trees: Detection, Estimation, and Modulation Theory, John Wiley, 2001.

16. Louis L. Scharf: Statistical Signal Processing: Detection, Estimation, and Time Series Analysis, Addison-Wesley, 1991

17. Amir Dembo, Ofer Zeitouni: Large Deviations Techniques and Applications, Springer, 2009

| Weekly Contact Hours                                | : 5 Lectur                    | <b>res:</b> 2                     | Practical work: 3                                 |    |
|---|-------------------------------|-----------------------------------|---|----|
| Teaching Methods:                                   |                               |                                   |   |    |
| Lectures; revisions of th<br>– colloquia; homeworks |                               | e students' participation in pro  | oblem solving; knowledge tests                    |    |
| Knowledge Assessment (maximum of 100 points): 100   |                               |                                   |   |    |
| Pre-exam obligations                                | points                        | Final exam                        | points  |    |
| Active class<br>participation                       |                               | written exam                      | 40  |    |
| Colloquia +<br>Homeworks                            | 30 (Colloquia)<br>(Homeworks) | + 30 oral exam                    |   |    |
| Preliminary exam(s)                                 |                               |                                   |   |    |
| Seminar(s)  |                               |                                   |   |    |
| The methods of knowled<br>project presentation, sen | 0                             | hay differ; the table presents of | only some of the options: written exam, oral exam | ı, |